Terahertz Signatures of Hydrate Formation in Alkali Halide Solutions

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ABSTRACT: We systematically studied the ability of 20 alkali halides to form solid hydrates in the frozen state from their aqueous solutions by terahertz time-domain spectroscopy combined with density functional theory (DFT) calculations. We experimentally observed the rise of new terahertz absorption peaks in the spectral range of 0.3–3.5 THz in frozen alkali halide solutions. The DFT calculations prove that the rise of observed new peaks in solutions containing Li⁺, Na⁺ or F⁻ ions indicates the formation of salt hydrates, while that in other alkali halide solutions is caused by the splitting phonon modes of the imperfectly crystallized salts in ice. As a simple empirical rule, the correlation between the terahertz signatures and the ability of 20 alkali halides to form a hydrate has been established.

TOC GRAPHICS:

The formation of salt hydrates is important in understanding diverse phenomena in chemistry and also is critical to many practical applications in geology, climatology and pharmacy. In geology, the identification of hydrates that are ubiquitous in glacier minerals such as hydrohalite can improve the understanding of diagenesis.¹⁻³ In astronomy, salt hydrates within saline deposits on Mars and Europa were found to be evidence of the presence of water.⁴⁻⁶ In climatology, hydrated salts have been proven to be better nuclei for cloud formation than nonhydrated salt particles.⁷⁻⁸ More generally, the nature of salt hydrates has widespread significance in the fields of biology and food science, such as cell survival under freeze-thawing⁹ and low-temperature preservation of biological tissues and foods.¹⁰⁻¹¹

Studies of salt hydrates conducted thus far include a number of different techniques, such as nuclear magnetic resonance (NMR),¹²,¹³ X-ray diffraction (XRD),¹⁴⁻¹⁷ and neutron diffraction,¹⁸⁻²⁰ where the crystal structures, the structural environments and the ratio of ions and water molecules of the salt hydrates can be evaluated. Infrared (IR) spectroscopy has also been widely utilized for investigations of hydrate formation in various aqueous salt solutions by cooling.²¹⁻²⁸ As it provides sensitivity to the high frequency O-H vibrational information, IR spectroscopy could be a useful tool in the characterization of structural changes during hydrate
With the recent advent of a new spectroscopic technique, terahertz time-domain spectroscopy (THz-TDS), the far-infrared lower frequency properties of materials in the range below 3.5 THz can be readily obtained.\textsuperscript{30,32} Unlike IR spectroscopy, terahertz spectra are more sensitive to molecular conformational and structural changes.\textsuperscript{31,33} In 2018, Ajiro and coauthors captured the appearance of new terahertz absorption peaks at around 1.5-1.6 and 2.3-2.4 THz during the formation process of NaCl hydrates and these peaks were assigned to the intermediate of NaCl hydrates.\textsuperscript{34} Our recent work also reported the observation of NaCl hydrate formation in aqueous solution and the preliminary results indicated that the formed NaCl hydrate produces new terahertz absorption peaks at around 1.6, 2.43, 3.34, and 3.78 THz.\textsuperscript{35} Here we systematically study the hydrate formation of 20 alkali halides from their aqueous solutions in the frozen state by using THz-TDS and explore the correlation of terahertz signatures with their ability to form hydrates.

In figures 1a-1e, the terahertz spectra of water and the first series of four chloride salt tablets (NaCl, KCl, RbCl, and CsCl) recorded at room temperature are shown by the dotted blue lines, and the corresponding spectra of their frozen aqueous solutions at 223 K are presented by the solid red lines. No remarkable terahertz absorption peaks are observed for either the liquid water or the ice over the frequency range of 0.3-3.5 THz, whereas the ice is more transparent than the liquid water due to the constrained thermal fluctuation of the hydrogen bonds. The low, smooth terahertz absorption of the ice is an ideal background for studying hydrate formation processes. Figure 1b illustrates the terahertz spectra of the solid NaCl tablet and the frozen aqueous NaCl solution. Compared with the terahertz spectrum of the solid NaCl tablet, new terahertz absorption peaks are observed at 1.60, 2.43, and 3.34 THz in the aqueous NaCl solution in the frozen state. Since these absorption peaks do not exist in the terahertz spectra of either the ice or the solid NaCl tablet, they arise entirely from the newly formed frozen structures. The direct evidence comes from the XRD measurements. A low-temperature (223 K) XRD experiment was implemented with the 1 mol/L NaCl solution, and the diffraction patterns are presented as orange lines in Figure 1g. Compared with ice (H\textsubscript{2}O Ih PDF: 85-0857) and NaCl crystals (NaCl PDF: 70-2509), there are obvious new diffraction peaks in the frozen NaCl solution, as indicated by the purple arrows in Figure 1g. The assignments of the measured XRD patterns suggest the newly formed structure: NaCl\textsubscript{2}H\textsubscript{2}O hydrate (NaCl\textsubscript{2}H\textsubscript{2}O PDF: 70-1158). Hence, it is evident that the observed terahertz absorption peaks are caused by the formed NaCl\textsubscript{2}H\textsubscript{2}O hydrate, and the characterized peaks originate from collective vibrations of all molecules in the hydrate crystal.\textsuperscript{36} The absorption peaks at 1.60 and 2.43 THz were also observed in frozen NaCl solution during the freeze-drying process. These two peaks were assigned to metastable unit-cell-sized distorted NaCl\textsubscript{2}H\textsubscript{2}O particles rather than the dihydrate NaCl\textsubscript{2}H\textsubscript{2}O crystals since NaCl\textsubscript{2}H\textsubscript{2}O has no dipole moment for inducing terahertz absorption peaks.\textsuperscript{37} However, the terahertz peak can also be contributed by the lattice vibration of the non-dipole -moment crystal. As discussed in ref. 35, these two peaks, together with the peak at 3.34 THz, were assigned ideally to the specific vibration forms of a hydrate crystal by DFT.

Now for the other salts in this series, i.e., KCl, RbCl, and CsCl, Figures 1c-e shows their measured terahertz spectra. It can be seen that all of the frozen aqueous KCl, RbCl, and CsCl solution samples display absorption profiles similar to those observed in their corresponding tablet samples. Unlike the case of NaCl, no additional terahertz absorption peaks are observed in the spectra below 3.5 THz in frozen aqueous KCl and RbCl solutions. This can be further confirmed by the XRD patterns illustrated in Figure 1b-i, where the diffraction peaks of the frozen aqueous salt solutions agree well with the superposed diffraction peaks of the ice and the salt crystal. The assignments of the measured XRD patterns clearly indicate that there is no new hydrated structure formed during freezing the aqueous KCl and RbCl solutions. One may notice that in CsCl solution a sharp peak at 3.07 THz appears in the frozen sample at 223 K. The appearance of this peak might be caused by two possible reasons. First, the formed hydrates produce the new absorption peaks, similar to that in the NaCl solution. Second, temperature and geometry effects in frozen solution give rise to the narrowed and red-shifted band at 3.07 THz compared with that of the CsCl tablet at 3.14 THz.\textsuperscript{36,37} The terahertz absorption peaks of both the CsCl tablet and frozen CsCl solution originate from lattice vibrations of the cubic crystal.\textsuperscript{38} Comparing the XRD patterns of the frozen CsCl solution with those of the CsCl tablet and the ice shown in Figure 1j, we found that the diffraction peaks of the frozen aqueous CsCl solutions agree well with the superposed diffraction peaks of the ice and the CsCl tablet. Hence, there are no new hydrated structures formed in the aqueous CsCl solutions upon freezing.
Comparing the terahertz spectra of the frozen salt molecules in the unit cell, and mainly comes at 39.40 at the origin of the modes observed in NaBr⋅2H₂O, containing salts NaBr, NaI, KBr, KI, RbBr, RbI, CsBr, and CsI.

Thus far, the terahertz studies of the first series of chloride salts have shown that the significant change in the terahertz spectrum with the emergence of discrete peaks provides visible indications of the salt hydrate formation. The result also implies that the sodium ion has a substantial effect on the salt hydrate formation compared to the other alkali ions K⁺, Rb⁺, and Cs⁺. To investigate the effects of different ions on the hydrate formation, we performed experiments on the second series containing salts NaBr, NaI, KBr, KI, RbBr, RbI, CsBr, and CsI.

To verify this speculation, we performed density functional theory (DFT) calculations on NaBr⋅2H₂O. The results are plotted in Figure 3, and the used parameters from ref. 39 are listed in the caption. The vibrational mode at 2.36 THz, corresponding to the peak at 2.11 THz in the experimental spectra, is assigned to the translational vibration of Na⁺, and Br⁻ ions and parts of the water molecules along the short diagonal at an angle of about ±45° with respect to the ac plane. The peak at 3.35 THz, corresponding to the experimental peak above 3.5 THz, can be assigned to the translational vibration of Na⁺, and Br⁻ ions and parts of the water molecules along the short diagonal at an angle of about ±45° with respect to the ac plane. The DFT calculation on NaBr⋅2H₂O confirms that the newly discovered terahertz absorption peaks in the frozen NaBr solution originate from the vibrational modes of the NaBr⋅2H₂O crystal. Similar to NaCl and NaBr solutions, other sodium halides also produce new terahertz absorption peaks in the frozen state. The terahertz features mainly originate from collective vibrations of molecules in hydrate crystals, and each feature has been marked as being part of a specific vibrational mode.

Figure 3. Theoretical calculation results of terahertz spectroscopy and the corresponded vibrational modes of NaBr⋅2H₂O. (a) Crystal structure of NaBr⋅2H₂O viewed along the c axis, with the enlarged frame showing a unit cell. The periodic boundary condition is employed in the calculation. The parameters of the unit cell are \( a = 6.570 \, \text{Å}, b = 10.380 \, \text{Å}, c = 6.780 \, \text{Å}, \beta = 113.5°, \) and \( \alpha = \gamma = 90°.\) Na⁺ and Br⁻ are represented by purple and brown balls, respectively. (b) Experimental and calculated terahertz spectra of NaBr⋅2H₂O. (c, d) Calculated vibrational modes of NaBr⋅2H₂O at (c) 2.36 THz and (d) 3.35 THz.
caused by the formation of hydrates and/or the distortion of the nonhydrated crystals. However, Iglev’s work in 2010 experimentally proved that CsBr and CsI salts do not form hydrates because of their high enthalpies of solution. Thus, these newly generated peaks are due to the lattice vibration of distorted CsBr and CsI crystals restricted in the local environment of surrounding ice. Similar lattice distortion has already been observed for nanocrystals and doped crystals. It is worth mentioning that in CsCl solution there is no phonon mode splitting observed in the frozen state. This is probably because of both the limitation of the available frequency region in the experiment and the instability of the tilted CsCl crystal compared with CsBr and CsI.

To theoretically investigate the origin of the freezing-induced peaks in these nonhydrated salts, we also performed DFT calculations, and the results of CsBr and CsI are plotted in Figure 4. For a distorted CsBr crystal with parameters of \( a = b = c = 4.163 \, \text{Å} \) and \( \alpha = \beta = \gamma = 88.7^\circ \), the features of the calculated spectra capture the terahertz experimental results well. The calculated vibrational mode at 2.27 THz matches the measured peak at 2.27 THz. This peak arises from the collective \( \text{Cs}^+ \) and \( \text{Br}^- \) ion vibrations in the short diagonal direction at an angle of about 45° to the \( ac \) plane (Figure 4c). The peak at 2.72 THz, corresponding to the experimental peak at 2.71 THz, is assigned to the same two energy vibrations lying in the short diagonal direction at an acute angle with respect to the \( ac \) plane (Figure 4d) and in the long diagonal direction at an acute angle with respect to the \( ac \) plane (Figure 4e).

Similarly, Figures 4f-j shows the theoretical calculation results of terahertz spectroscopy and the corresponding vibrational modes of the CsI imperfect crystal, and the parameters of the CsI crystal structure are \( a = b = c = 4.410 \, \text{Å}, \alpha = 90^\circ, \beta = 91.7^\circ, \) and \( \gamma = 93^\circ \). The calculation captured the terahertz experimental results well. These absorption peaks

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**Figure 4.** Theoretical calculation results of terahertz spectroscopy and the corresponding vibrational modes of (a-e) CsBr and (f-j) CsI. The crystal structures of CsBr and CsI, and periodic boundary condition are employed in the calculation. The parameters of the unit cell are (a) \( a = b = c = 4.163 \, \text{Å} \), and \( \alpha = \beta = \gamma = 88.7^\circ \) and (f) \( a = b = c = 4.410 \, \text{Å}, \alpha = 90^\circ, \beta = 91.7^\circ, \) and \( \gamma = 93^\circ \). \( \text{Cs}^+, \text{Br}^- \) and \( \text{I}^- \) are represented by purple-black, brown and pink balls, respectively. Experimental and calculated terahertz spectra of (b) CsBr and (g) CsI. Calculated vibrational modes of CsBr at (c) 2.27 THz and (d-e) 2.72 THz and of CsI at (h) 1.90 THz, (i) 2.25 THz, and (j) 2.65 THz.

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**Figure 5.** Terahertz spectra of lithium halides and alkali fluorides: the dotted blue lines and continuous red lines represent solid salts at room temperature and the frozen aqueous salts, respectively.
originates from the lattice vibration of a distorted CsI crystal with different energies in three vibrational directions. The good agreement between the calculated spectra terahertz of distorted nonhydrated crystals and the measured spectra of frozen solutions confirms that the newly discovered terahertz absorption peaks in the frozen CsBr and CsI solutions are derived from the lattice vibration of the imperfect crystals rather than the hydrate solution. These two salt solutions are prone to lattice distortion in the frozen state, which may be due to the large atomic radius of these ions making them easy to deform. These results also verify that the Br− and I− anions do not have a visible influence on the formation of salt hydrates, while alkali cation Na+ still has important roles.

In addition to the above alkali halides, our study is carried out on the third series containing salts LiF, LiCl, LiBr, LiI, NaF, KF, RbF, and CsF. The influence of F− and Li+ ions on the salt hydrate formation is further investigated. Different from the salts in the first and second series, the lithium and fluoride salts show some specific features. Salt LiF has very poor water solubility. The unsaturated lithium salt solutions of LiCl, LiBr, and LiI, such as at 1 mol/L, are prone to supercooling in our freezing experiments even if the temperature drops to the limit of our equipment, 80 K. However, their saturated solutions are easy to nucleate and crystallize during the freezing process due to supersaturation. Similarly, the fluoride salt solutions of NaF and CsF at the saturated concentrations are also used in our experiment to avoid supercooling. The KF and RbF solutions are adopted at the same concentration of 1 mol/L as in the previous series. Figure 5 presents the terahertz spectra of the salt samples in the third series. Except for LiF, newly emerging peaks are observed in all of the lithium halide solutions and alkali fluoride solutions in the frozen state. The distinct differences between the spectra of salt tablets and the frozen solutions indicate hydrate formation. This is also consistent with the previous report,44 where these lithium and fluoride salts do form hydrates. These results reveal that ions Li+ and F− also play substantial roles in salt hydrate formation.

Finally, we studied the effects of the cooling rate and concentration on the formation of salt hydrates. To investigate the effects of the cooling rate on the formation of hydrates, we monitored the changes in terahertz spectra of a fast-frozen NaCl aqueous sample during warm up. The fast-frozen sample was prepared by soaking it into liquid nitrogen directly, and the temperature dropped from room temperature to 80 K within 2 min. The measured spectra are presented in Figure S1a, and for comparison, the spectra of a 1 mol/L NaCl aqueous solution during slow cooling is also inserted into Figure S1b. There is no absorption peak in fast cooling at 80 K due to the formation of the amorphous hydrate while the temperature increases up to 110 K, producing absorption peaks at about 1.6, 2.4, and 3.3 THz, and up 110 K due to the transformation of hydrate from amorphous to crystal. These peaks are generally consistent with slower cooling and are slightly shifted due to the temperature change. Although, freezing rate has certain effects on the formation of salt hydrate, the obtained salt hydrates are the same in slow and fast cooling processes. In our recent results, the terahertz spectra of NaCl solutions with different concentrations at 223 K were recorded.35 At lower concentrations of 0.1-0.3 mol/L, the peak is invisible due to the detection limit of the terahertz detector. When the concentration is larger than 1.0 mol/L, we could see clearly the terahertz absorption peaks at 1.60, 2.43, and 3.34 THz, indicating the formation of the NaCl hydrate. Thus, there is no obvious effect of concentration on the formation of hydrates in our study.

Thus far, in terms of our terahertz measurements, the ability of 20 alkali halide solutions to form hydrates in the frozen state has been summarized in Table 1. The numbers in Table 1 indicate the absorption peaks of the alkali halide solutions in the frozen state, the numbers in parentheses refer to the absorption peaks of the nonhydrate salt tablets, and the stars (★) in unit cells indicate the salts that can form hydrates. Most notably, the data in Table 1 clearly show that Na+, Li+, and F− ions play key roles in salt hydrate formation, and all lithium halides, sodium halides, and alkali fluorides are able to form hydrates upon cooling their aqueous solutions except for LiF due to its poor water solubility. However, the nine other salts cannot form hydrates during the freezing process. Our observations here are also consistent with those reported previously using IR spectroscopy.44

The key factor in determining whether a salt could form hydrates is the ion-water binding energy. The potential energy of the interaction between the full charge of an ion and the two partial charges of a water molecule is $E_p \propto (\frac{\mu}{r^2}$, where $z$ is the charge number of the ion, $\mu$ is the electric dipole moment of the water molecule, and $r$ is the distance between the ion and the dipole, which is larger for a larger ion radius.45 Thus, it is obvious that the binding energy of the ions is closely related to the ionic radius. The ionic radii are: Li+ (76 pm) <Na+ (102 pm) <F− (133 pm) <K+ (138 pm) <Rb+ (152 pm) <Cs+ (167 pm) <Cl− (181 pm) <Br− (196 pm) <I− (220 pm).46 For the same amount of charge, the smaller ion radius corresponds to a stronger binding energy of ion-water. The first binding energies of Li+, Na+, and F− ions to water molecules are 34, 24 and 23.3 kcal/mol, respectively.46 The binding energies of these ions are stronger than the total binding energy of 22.2 kcal/mol for the four saturated hydrogen bonds of each H2O in Ih ice.47 Thus, even at the eutectic temperature where these ions are recombined with other oppositely charged ions, the strongly

<table>
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<tr>
<th>Ion</th>
<th>Salt (Solubility)</th>
<th>F− Peaks</th>
<th>Cl− Peaks</th>
<th>Br− Peaks</th>
<th>I− Peaks</th>
</tr>
</thead>
<tbody>
<tr>
<td>Na+</td>
<td>NaF 3.30</td>
<td>★</td>
<td>NaCl 1.60, 2.43, 3.34</td>
<td>★ NaBr 2.11</td>
<td>★ NaI 1.25, 1.68</td>
</tr>
<tr>
<td>K+</td>
<td>KF 1.61, 2.29, 2.53, 2.85</td>
<td>★</td>
<td>KCl</td>
<td>KBr</td>
<td>KI 3.13 (3.17)</td>
</tr>
<tr>
<td>Rb+</td>
<td>RbF 0.75, 1.14, 1.98, 2.56</td>
<td>★</td>
<td>RbCl</td>
<td>RbBr 2.69 (2.75)</td>
<td>RbI 2.30 (2.31)</td>
</tr>
<tr>
<td>Cs+</td>
<td>CsF 1.28, 2.11, 2.93</td>
<td>★</td>
<td>CsCl 3.07 (3.14)</td>
<td>CsBr 2.27, 2.71 (2.24)</td>
<td>CsI 1.90, 2.25 (1.90)</td>
</tr>
</tbody>
</table>

Table 1. Terahertz Absorption Peaks of Alkali Halide Solutions in the Frozen States.
bonded water molecules remain and are complementarily filled into their lattice vacancies to make the system the most stable (to minimize the Gibbs free energy of the system), and thereby form a salt hydrate. For example, for the NaCl solution, the binding energy of Na\(^+\) is high enough to interact with the hydrating water molecules to develop many micro NaCl\(\cdot\)2\(\text{H}_2\text{O}\) crystals.\(^6\) However, for K\(^+\), Rb\(^+\), Cs\(^+\), Cl\(^-\), Br\(^-\) and I\(^-\) ions, the first ion-water binding energies are 17.9, 15.9, 13.7, 13.1, 12.6 and 10.6 kcal/mol, respectively. These binding energies are smaller than the binding energy of ice.\(^7\) As a result, these ions are extruded out of the hydrogen bond networks and tend to form many micro nonhydrated salt crystals.

In conclusion, the ability of 20 alkali halide solutions to form hydrates in the frozen state has been studied by terahertz time-domain spectroscopy. The distinct change in the terahertz spectrum with the emergence of discrete peaks of the salt solutions in the frozen states has been demonstrated to provide a direct and visible indication of salt hydrate formation. The study revealed that alkali metal cations Na\(^+\) and Li\(^+\) have substantial effects on the salt hydrate formation, which can aid the higher first binding energies of these three ions with water, and they benefit the hydrate-formation process. These observations would therefore establish a simple and conceivable correlation between the terahertz signatures and the salt hydrate formation. Given the extraordinary sensitivity of terahertz spectroscopy, it is believed that such a technique could provide more possibilities for investigations of other hydrate formation systems with different solvents or solutes.

**ASSOCIATED CONTENT**

**Supporting Information**

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**Notes**

The authors declare no competing financial interest.

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